

B-22 単項式と多項式の乗法と除法

正答数

/8

● 次の計算をしなさい。

$$\textcircled{1} \quad 3a(2b + 1)$$

$$= 6ab + 3a$$

$$\textcircled{2} \quad -4x(2x + 5y)$$

$$= -8x^2 - 20xy$$

$$\textcircled{3} \quad (4ab - 12a) \div 2a$$

$$= 2b - 6$$

$$\textcircled{4} \quad (-36x^2 + 9x) \div (-3x)$$

$$= 12x - 3$$

$$\textcircled{5} \quad (20a + 35b) \times \left(-\frac{1}{5}a\right)$$

$$= -4a^2 - 7ab$$

$$\textcircled{6} \quad (6a^2 - 4ab) \div \frac{1}{2}a$$

$$= 12a - 8b$$

$$\textcircled{7} \quad 5y(2x + 3y - z)$$

$$= 10xy + 15y^2 - 5yz$$

$$\textcircled{8} \quad (6x^3 - 4x^2y) \div \frac{2}{3}x$$

$$= 9x^2 - 6xy$$

B-23 式の展開

正答数

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● 次の式を展開しなさい。

① $(a+1)(2a+5)$

$$= 2a^2 + 7a + 5$$

② $(3x+1)(x-3)$

$$= 3x^2 - 8x - 3$$

③ $(1+3a)(4-2a)$

$$= -6a^2 + 10a + 4$$

④ $(x-3)(1-2x)$

$$= -2x^2 + 7x - 3$$

⑤ $(3x+2y)(x+6y)$

$$= 3x^2 + 20xy + 12y^2$$

⑥ $(a+4b)(2a-b)$

$$= 2a^2 + 7ab - 4b^2$$

⑦ $(4a-3b)(a+4b)$

$$= 4a^2 + 13ab - 12b^2$$

⑧ $(-x+3y)(3x-5y)$

$$= -3x^2 + 14xy - 15y^2$$

B-24 $(x+a)(x+b)$ の展開

正答数

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組 番 名前

● 次の式を展開しなさい。

① $(x+3)(x+2)$

$$= x^2 + 5x + 6$$

② $(x+1)(x+8)$

$$= x^2 + 9x + 8$$

③ $(a-4)(a+1)$

$$= a^2 - 3a - 4$$

④ $(x-2)(x+6)$

$$= x^2 + 4x - 12$$

⑤ $(x+5)(x-9)$

$$= x^2 - 4x - 45$$

⑥ $(a+7)(a-2)$

$$= a^2 + 5a - 14$$

⑦ $(x-5)(x-6)$

$$= x^2 - 11x + 30$$

⑧ $(x-3)(x-9)$

$$= x^2 - 12x + 27$$

B-25 $(x+a)^2$, $(x-a)^2$ の展開

正答数

組 番 名前

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● 次の式を展開しなさい。

① $(x+3)^2$
 $= x^2 + 6x + 9$

② $(x+4)^2$
 $= x^2 + 8x + 16$

③ $(a+1)^2$
 $= a^2 + 2a + 1$

④ $(6+a)^2$
 $= a^2 + 12a + 36$

⑤ $(x-2)^2$
 $= x^2 - 4x + 4$

⑥ $(x-10)^2$
 $= x^2 - 20x + 100$

⑦ $(a-9)^2$
 $= a^2 - 18a + 81$

⑧ $(a-5)^2$
 $= a^2 - 10a + 25$

B-26 $(x+a)(x-a)$ の展開

正答数

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組 番 名前

● 次の式を展開しなさい。

① $(x+9)(x-9)$

$$= x^2 - 81$$

② $(x+5)(x-5)$

$$= x^2 - 25$$

③ $(x-6)(x+6)$

$$= x^2 - 36$$

④ $(x-4)(x+4)$

$$= x^2 - 16$$

⑤ $(1+x)(1-x)$

$$= 1 - x^2$$

⑥ $(3-a)(3+a)$

$$= 9 - a^2$$

⑦ $(x-y)(x+y)$

$$= x^2 - y^2$$

⑧ $\left(x+\frac{1}{3}\right) \left(x-\frac{1}{3}\right)$

$$= x^2 - \frac{1}{9}$$

B-27 いろいろな式の展開①

正答数

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● 次の式を展開しなさい。

① $(2x+3)(2x-1)$

$$= 4x^2 + 4x - 3$$

② $(4x+5)^2$

$$= 16x^2 + 40x + 25$$

③ $(3a-1)^2$

$$= 9a^2 - 6a + 1$$

④ $(5x+2)(5x-2)$

$$= 25x^2 - 4$$

⑤ $(4x+y)(4x-y)$

$$= 16x^2 - y^2$$

⑥ $(6a+7b)(6a-7b)$

$$= 36a^2 - 49b^2$$

⑦ $(x+1)(x-3) + (x+5)^2$

$$= x^2 - 2x - 3 + x^2 + 10x + 25$$

$$= 2x^2 + 8x + 22$$

⑧ $(a+2)(a-1) - (a+2)(a-2)$

$$= a^2 + a - 2 - (a^2 - 4)$$

$$= a + 2$$

B-28 いろいろな式の展開②

正答数

組 番 名前

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● 次の式を展開しなさい。

$$\begin{aligned} \textcircled{1} \quad & (x - 3y)(x - 3y + 8) \\ & = M(M + 8) \\ & = M^2 + 8M \\ & = (x - 3y)^2 + 8(x - 3y) \\ & = x^2 - 6xy + 9y^2 + 8x - 24y \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad & (x + y + 5)(x + y - 2) \\ & = (M + 5)(M - 2) \\ & = M^2 + 3M - 10 \\ & = (x + y)^2 + 3(x + y) - 10 \\ & = x^2 + 2xy + y^2 + 3x + 3y - 10 \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad & (x - 2y + 4)^2 \\ & = (M + 4)^2 \\ & = M^2 + 8M + 16 \\ & = (x - 2y)^2 + 8(x - 2y) + 16 \\ & = x^2 - 4xy + 4y^2 + 8x - 16y + 16 \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad & (x - y + 7)(x - y - 7) \\ & = (M + 7)(M - 7) \\ & = M^2 - 7^2 \\ & = (x - y)^2 - 49 \\ & = x^2 - 2xy + y^2 - 49 \end{aligned}$$

$$\begin{aligned} \textcircled{5} \quad & (a + b + 1)(a - b + 1) \\ & = (a + 1 + b)(a + 1 - b) \\ & = (M + b)(M - b) \\ & = M^2 - b^2 \\ & = (a + 1)^2 - b^2 \\ & = a^2 + 2a + 1 - b^2 \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad & (x + 3y - 2)(x - 3y + 2) \\ & = \{x + (3y - 2)\}\{x - (3y - 2)\} \\ & = (x + M)(x - M) \\ & = x^2 - M^2 \\ & = x^2 - (3y - 2)^2 \\ & = x^2 - (9y^2 - 12y + 4) \\ & = x^2 - 9y^2 + 12y - 4 \end{aligned}$$

B-29 因数分解①

組 番 名前

正答数

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● 次の式を因数分解しなさい。

① $3x + 15$

$= 3(x + 5)$

② $4a - 6b$

$= 2(2a - 3b)$

③ $10xy + 5x$

$= 5x(2y + 1)$

④ $18a^2 - 12a$

$= 6a(3a - 2)$

⑤ $2xy + xy^2$

$= xy(2 + y)$

⑥ $21a^2b - 14ab^2$

$= 7ab(3a - 2b)$

⑦ $3x^2y - 12xy^2 + 9x$

$= 3x(xy - 4y^2 + 3)$

⑧ $6a^2b + 8b - 4b^2$

$= 2b(3a^2 + 4 - 2b)$

B-30 因数分解②

正答数

組 番 名前

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● 次の式を因数分解しなさい。

$$\begin{aligned} \textcircled{1} \quad & x^2 + 4x + 3 \\ & = (x+3)(x+1) \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad & x^2 + 6x + 8 \\ & = (x+4)(x+2) \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad & a^2 - 8a + 15 \\ & = (a-3)(a-5) \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad & x^2 - 5x + 6 \\ & = (x-2)(x-3) \end{aligned}$$

$$\begin{aligned} \textcircled{5} \quad & a^2 + 5a - 14 \\ & = (a+7)(a-2) \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad & x^2 + 7x - 30 \\ & = (x+10)(x-3) \end{aligned}$$

$$\begin{aligned} \textcircled{7} \quad & x^2 - 3x - 40 \\ & = (x+5)(x-8) \end{aligned}$$

$$\begin{aligned} \textcircled{8} \quad & a^2 - 2a - 48 \\ & = (a+6)(a-8) \end{aligned}$$

B-31 因数分解③

正答数

組 番 名前

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● 次の式を因数分解しなさい。

① $x^2 + 4x + 4$

$= (x + 2)^2$

② $x^2 + 16x + 64$

$= (x + 8)^2$

③ $a^2 + 10a + 25$

$= (a + 5)^2$

④ $x^2 + 14x + 49$

$= (x + 7)^2$

⑤ $a^2 - 6a + 9$

$= (a - 3)^2$

⑥ $x^2 - 2x + 1$

$= (x - 1)^2$

⑦ $x^2 - 12x + 36$

$= (x - 6)^2$

⑧ $x^2 - 8x + 16$

$= (x - 4)^2$

B-32 因数分解④

正答数

組 番 名前

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● 次の式を因数分解しなさい。

① $x^2 - 1$
 $= (x + 1)(x - 1)$

② $x^2 - 9$
 $= (x + 3)(x - 3)$

③ $x^2 - 49$
 $= (x + 7)(x - 7)$

④ $x^2 - 16$
 $= (x + 4)(x - 4)$

⑤ $x^2 - 25$
 $= (x + 5)(x - 5)$

⑥ $x^2 - 64$
 $= (x + 8)(x - 8)$

⑦ $x^2 - 81$
 $= (x + 9)(x - 9)$

⑧ $x^2 - 36$
 $= (x + 6)(x - 6)$

B-33 因数分解⑤

正答数

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● 次の式を因数分解しなさい。

$$\begin{aligned} \textcircled{1} \quad & x^2 + 12xy + 36y^2 \\ & = (x + 6y)^2 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad & 9x^2 - 12x + 4 \\ & = (3x - 2)^2 \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad & 81a^2 - 1 \\ & = (9a + 1)(9a - 1) \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad & 25x^2 - 36y^2 \\ & = (5x + 6y)(5x - 6y) \end{aligned}$$

$$\begin{aligned} \textcircled{5} \quad & 2a^2 + 8a + 6 \\ & = 2(a^2 + 4a + 3) \\ & = 2(a + 3)(a + 1) \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad & 3x^2 + 9x - 30 \\ & = 3(x^2 + 3x - 10) \\ & = 3(x + 5)(x - 2) \end{aligned}$$

$$\begin{aligned} \textcircled{7} \quad & 6x^2 - 24xy + 24y^2 \\ & = 6(x^2 - 4xy + 4y^2) \\ & = 6(x - 2y)^2 \end{aligned}$$

$$\begin{aligned} \textcircled{8} \quad & 2a^2 - 18b^2 \\ & = 2(a^2 - 9b^2) \\ & = 2(a + 3b)(a - 3b) \end{aligned}$$

B-34 因数分解⑥

正答数

組 番 名前

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● 次の式を因数分解しなさい。

$$\textcircled{1} \quad (x+2)^2 - 3(x+2)$$

$$= M^2 - 3M$$

$$= M(M-3)$$

$$= (x+2)(x+2-3)$$

$$= (x+2)(x-1)$$

$$\textcircled{2} \quad (x-5)^2 + 8(x-5) + 16$$

$$= M^2 + 8M + 16$$

$$= (M+4)^2$$

$$= (x-5+4)^2$$

$$= (x-1)^2$$

$$\textcircled{3} \quad (x+7)^2 - 49$$

$$= M^2 - 7^2$$

$$= (M+7)(M-7)$$

$$= (x+7+7)(x+7-7)$$

$$= x(x+14)$$

$$\textcircled{4} \quad (2x+1)^2 + 5(2x+1)-6$$

$$= M^2 + 5M - 6$$

$$= (M+6)(M-1)$$

$$= (2x+1+6)(2x+1-1)$$

$$= 2x(2x+7)$$

$$\textcircled{5} \quad xy + 6x + y + 6$$

$$= x(y+6) + (y+6)$$

$$= (x+1)(y+6)$$

$$\textcircled{6} \quad ab - 9a - b + 9$$

$$= a(b-9) - (b-9)$$

$$= (a-1)(b-9)$$

$$\textcircled{7} \quad xy + 12y - 5x - 60$$

$$= y(x+12) - 5(x+12)$$

$$= (x+12)(y-5)$$

$$\textcircled{8} \quad 18xy + 12x + 21y + 14$$

$$= 6x(3y+2) + 7(3y+2)$$

$$= (6x+7)(3y+2)$$

B-35 式の計算の活用

正答数

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1 乗法公式を使って、次の計算をしなさい。

$$\begin{aligned} \textcircled{1} \quad & 104 \times 96 \\ & = (100 + 4)(100 - 4) \\ & = 100^2 - 4^2 \\ & = 9984 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad & 47 \times 53 \\ & = (50 - 3)(50 + 3) \\ & = 50^2 - 3^2 \\ & = 2491 \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad & 42^2 \\ & = (40 + 2)^2 \\ & = 1600 + 160 + 4 \\ & = 1764 \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad & 199^2 \\ & = (200 - 1)^2 \\ & = 40000 - 400 + 1 \\ & = 39601 \end{aligned}$$

2 因数分解の公式を使って、次の計算をしなさい。

$$\begin{aligned} \textcircled{1} \quad & 57^2 - 43^2 \\ & = (57 + 43)(57 - 43) \\ & = 100 \times 14 \\ & = 1400 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad & 35^2 - 15^2 \\ & = (35 + 15)(35 - 15) \\ & = 50 \times 20 \\ & = 1000 \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad & 85^2 - 84^2 \\ & = (85 + 84)(85 - 84) \\ & = 169 \times 1 \\ & = 169 \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad & 201^2 - 200^2 \\ & = (201 + 200)(201 - 200) \\ & = 401 \times 1 \\ & = 401 \end{aligned}$$